diagram, Fig. 2. Bond distances and angles for the structure are presented in Table 3. Atoms of the type $\mathrm{Cd}(1)$ and $\mathrm{Cd}(2)$ occupy centres of symmetry, on the space group special positions $(a)$ and (d) respectively, to form a face-centred array which the formate ligands $A$ and $B(A$ and $B$ refer to

$$
\begin{gathered}
\stackrel{\mathrm{H}(1)}{\stackrel{H}{\mathrm{C}}} \underset{\mathrm{C}(1)-\mathrm{O}(2)}{\mathrm{O}(1)} \text { and } \mathrm{O}(3)-\stackrel{\stackrel{H}{\mathrm{C}}(2)-\mathrm{O}(4)}{ } \mathrm{respectively)}
\end{gathered}
$$

bridge in the following manner. Ligand $A$ coordinates $\mathrm{Cd}(1)$ atoms alone, in anti-anti configuration, and links them into two-dimensional layers parallel to $b c$. Ligand B, which exhibits anti-syn configuration, bridges $\mathrm{Cd}(1)$ and $\mathrm{Cd}(2)$ atoms in planes parallel to $a b$, forming the three-dimensional polymeric lattice. $\mathrm{Cd}(1)$ is sixcoordinate through atoms $\mathrm{O}\left(1^{i}\right)$ and $\mathrm{O}(2)$ of ligand $A$ and $O(4)$ of $B$ (plus symmetry-related atoms), while $\mathrm{Cd}(2)$ completes its coordination sphere with $\mathrm{O}(3)$ from ligand $B$ and coordinated water molecules $\mathrm{O}(5)$ and $O(6)$. The polymer is further strengthened by the formation of hydrogen bonds between the water molecules and each of the formate oxygen atoms (Table 4).

Table 3. Bond distances $(\AA)$ and angles $\left({ }^{\circ}\right)$ with standard deviations in parentheses

| $\mathrm{Cd}(1)-\mathrm{O}(2)$ | $2 \cdot 248$ (4) | $\mathrm{C}(2)-\mathrm{O}(3)$ | $1 \cdot 224$ (8) |
| :---: | :---: | :---: | :---: |
| $\mathrm{Cd}(1)-\mathrm{O}(4)$ | $2 \cdot 301$ (5) | $\mathrm{C}(2)-\mathrm{O}(4)$ | $1 \cdot 251$ (8) |
| $\mathrm{Cd}(1)-\mathrm{O}\left(1^{\text {i }}\right.$ ) | $2 \cdot 263$ (4) | $\mathrm{C}(1)-\mathrm{H}(1)$ | 1.09 |
| $\mathrm{Cd}(2)-\mathrm{O}(3)$ | $2 \cdot 326$ (5) | $\mathrm{C}(2)-\mathrm{H}(2)$ | 1.06 |
| $\mathrm{Cd}(2)-\mathrm{O}(5)$ | $2 \cdot 298$ (5) | $\mathrm{O}(5)-\mathrm{H}(3)$ | 1.06 |
| $\mathrm{Cd}(2)-\mathrm{O}(6)$ | $2 \cdot 243$ (5) | $\mathrm{O}(5)-\mathrm{H}(4)$ | 1.09 |
| $\mathrm{C}(1)-\mathrm{O}(1)$ | 1.231 (8) | $\mathrm{O}(6)-\mathrm{H}(5)$ | 0.95 |
| $\mathrm{C}(1)-\mathrm{O}(2)$ | 1.230 (7) | $\mathrm{O}(6)-\mathrm{H}(6)$ | 1.03 |
| $\mathrm{O}(2)-\mathrm{Cd}(1)-\mathrm{O}(4)$ | 92.9 (2) | $\mathrm{Cd}(1)-\mathrm{O}(4)-\mathrm{C}(2)$ | $128 \cdot 5$ (4) |
| $\mathrm{O}(2)-\mathrm{Cd}(1)-\mathrm{O}\left(1^{1}\right)$ | $90 \cdot 5$ (2) | $\mathrm{O}(3)-\mathrm{C}(2)-\mathrm{O}(4)$ | $127 \cdot 0$ (7) |
| $\mathrm{O}(4)-\mathrm{Cd}(1)-\mathrm{O}\left(1^{1}\right)$ | $87 \cdot 7$ (2) | $\mathrm{Cd}(2)-\mathrm{O}(3)-\mathrm{C}(2)$ | $130 \cdot 0$ (5) |
| $\mathrm{O}(3)-\mathrm{Cd}(2)-\mathrm{O}(5)$ | 87.5 (2) | $\mathrm{O}(1)-\mathrm{C}(1)-\mathrm{H}(1)$ |  |
| $\mathrm{O}(3)-\mathrm{Cd}(2)-\mathrm{O}(6)$ | $89 \cdot 6$ (2) | $\mathrm{O}(2)-\mathrm{C}(1)-\mathrm{H}(1)$ | 118 |
| $\mathrm{O}(5)-\mathrm{Cd}(2)-\mathrm{O}(6)$ | $90 \cdot 1$ (2) | $\mathrm{O}(3)-\mathrm{C}(2)-\mathrm{H}(2)$ | 120 |
| $\mathrm{Cd}\left(1^{\mathrm{i}}\right)-\mathrm{O}\left(1^{\mathrm{t}}\right)-\mathrm{Cd}(1)$ | $125 \cdot 4$ (4) | $\mathrm{O}(4)--\mathrm{C}(2)-\mathrm{H}(2)$ |  |
| $\mathrm{O}(1)-\mathrm{C}(1)-\mathrm{O}(2)$ | $127 \cdot 6$ (6) | $\mathrm{H}(3)--\mathrm{O}(5)-\mathrm{H}(4)$ |  |
| $\mathrm{C}(1)-\mathrm{O}(2) \cdots-\mathrm{Cd}(1)$ | $122 \cdot 2$ (4) | $\mathrm{H}(5)-\mathrm{O}(6)-\mathrm{H}(6)$ | 106 |

Each coordination polyhedron is very close to regular octahedral (Table 3) and the variation in $\mathrm{Cd}-$ $O$ distance $[2 \cdot 243(5)-2 \cdot 326(5) \AA]$ is within the range

Table 4. Hydrogen-bond distances $(\AA)$ and angles $\left({ }^{\circ}\right)$

| $\mathrm{O}(5)-\mathrm{H}(3)-\mathrm{O}\left(2^{1 i}\right)$ | 128 | $\mathrm{O}(5) \cdots \mathrm{O}\left(2^{\text {ii }}\right)$ | $2.769(7)$ |
| :--- | :--- | :--- | :--- |
| $\mathrm{O}(5)-\mathrm{H}(4)-\mathrm{O}(4)$ | 118 | $\mathrm{O}(5) \cdots \mathrm{O}(4)$ | $2.748(7)$ |
| $\mathrm{O}(6)-\mathrm{H}(5)-\mathrm{O}\left(1^{1 i 1}\right)$ | 157 | $\mathrm{O}(6) \cdots \mathrm{O}\left(1^{\text {ii }}\right)$ | $2.773(8)$ |
| $\mathrm{O}(6)-\mathrm{H}(6)-\mathrm{O}\left(3^{1 i 1}\right)$ | 175 | $\mathrm{O}(6) \cdots \mathrm{O}\left(3^{\text {iii }}\right)$ | $2.721(7)$ |

Superscripts refer to the following symmetry-related positions:

| (i) | $x$ | $\frac{1}{2}-y$ | $\frac{1}{2}+z$ |
| ---: | ---: | ---: | ---: |
| (ii) | $x$ | $1+y$ | $z$ |
| (iii) | $1-x$ | $\frac{1}{2}+y$ | $\frac{1}{2}-z$ |

found with other cadmium carboxylates (Harrison \& Trotter, 1972; Post \& Trotter, 1974a, b, c). The longer distances $\mathrm{Cd}(1)-\mathrm{O}(4)$ and $\mathrm{Cd}(2)-\mathrm{O}(3)$ probably reflect the more sterically restrictive requirements imposed upon ligand $B$ in bridging between $\mathrm{Cd}(1)$ and $\mathrm{Cd}(2)$ layers, although residual charge upon the metal atoms [ $\mathrm{Cd}(1)$ is coordinated by six formate oxygen atoms and $\mathrm{Cd}(2)$ by only two] could be a contributing factor (Post \& Trotter, 1974b). The residual charge effect could also produce the longer $\mathrm{C}(2)-\mathrm{O}(4)$ bond $(1 \cdot 251$ $\AA$ ). Cd(2) may be expected to possess slight positive charge and, therefore, necessitate greater electron donation from $\mathrm{O}(3)$ than would be the case of donation from $\mathrm{O}(4)$ to $\mathrm{Cd}(1)$. In ligand $B$, a withdrawal of electrons into the bond $\mathrm{C}(2)-\mathrm{O}(3)$, to facilitate such a trend toward neutralization of charge, would have a weakening effect upon the bond $\mathrm{C}(2)-\mathrm{O}(4)$.

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# Refinement of the Crystal Structure of $\mathrm{NaInSi}_{2} \mathrm{O}_{6}$ 

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[^0]$c=5.3589$ (2) $\AA, \beta=107 \cdot 200(1)^{\circ}$. The variation in cell dimensions across the Na pyroxene series is linear with

the exception of $\mathrm{NaInSi}_{2} \mathrm{O}_{6}$ due to constraints applied by the M2 cation and elements of the tetrahedral chain on the rate of increase in the $a \sin \beta$ and $c$ dimensions.

Introduction. The variation in cell volume of the Na pyroxenes is linear with the cube of the M1 cation radius (Prewitt \& Shannon, 1969), except for $\mathrm{NaInSi}_{2} \mathrm{O}_{6}$, the cell volume of which is smaller than expected (Christiansen \& Hazell, 1967). This refinement was made in order to allow a detailed comparison with the other isomorphous Na pyroxenes.

The crystal used was provided by Dr Jun Ito of Harvard University. Precession photographs showed monoclinic symmetry and reflexions with $h+k=2 n+$ $1(h k l)$ and $l=2 n+1(h 0 l, 0 k l)$ were absent, consistent with the space group $C 2 / c$ observed for other Na pyroxenes (Prewitt \& Burnham, 1966; Clark, Appleman \& Papike, 1969). Experimental procedure and data-reduction methods are given by Hawthorne \& Grundy (1973). 969 intensities were collected, of which 902 were observed and used in the refinement.

After several cycles of least-squares refinement in which a scale factor and all symmetry-allowable positional parameters and temperature factors [of the form $\left.\exp \left(-\sum_{i=1}^{3} \sum_{j=1}^{3} h_{i} k_{j} \beta_{i j}\right)\right]$ were included as variables, the structure converged with conventional and weighted (unit weights) $R$ values of $2 \cdot 4 \%, 2 \cdot 6 \%$ for observed re-


Fig. 1. Variation of cell dimension with M1 cation (X) radius for the Na pyroxenes $\left(\mathrm{NaXSi}_{2} \mathrm{O}_{6}\right)$.

Table 2. Selected interatomic distances in $\mathrm{NaInSi}_{2} \mathrm{O}_{6}(\AA)$

| Si tetrahedron |  | M1 octahedron |  |
| :---: | :---: | :---: | :---: |
| SiA1-O1A1 | $1 \cdot 632$ (3) | M1-O1A1, B1 | 2.211 (2) |
| SiA1-O2A1 | 1.592 (2) | M1-O1A2, B2 | $2 \cdot 141$ (5) |
| SiA1-O3A1 | $1 \cdot 649$ (3) | M1-O2C1, D1 | 2.071 (2) |
| SiA1-O3A2 | 1.655 (3) | Mean | 2.141 |
| Mean | $1 \cdot 632$ |  |  |
|  |  | O1A1-O1B1 | $2 \cdot 857$ (6) |
| O1A1-O2A1 | $2 \cdot 723$ (4) | O2C1-O2D1 | $3 \cdot 121$ (5) |
| O1A1-03A1 | 2.655 (4) | O1A1-O2Cl | 3.051 (3) |
| O1A1-03A2 | 2.663 (7) | O1A1-O1A2 | 3.047 (2) |
| O2A1-03A1 | $2 \cdot 661$ (3) | O1A1-02Cl | $3 \cdot 058$ (3) |
| O2A1-03A2 | 2.593 (3) | O1A2-O2D1 | $3 \cdot 118$ (6) |
| O3A1-03A2 | 2.688 (1) | O1A1-O1B2 | $2 \cdot 840$ (7) |
| Mean | 2.664 |  | 3.017 |


| M2 antiprism |  |
| :--- | :--- |
| M2-O1A1, O1B1 1 | $2 \cdot 494(3)$ |
| M2-O2C2, O2D2 | $2.367(6)$ |
| M2-O3C1, O3D1 | $2.510(4)$ |
| M2-O3C2, O3D2 | $2.899(3)$ |
| Mean for 6 | 2.457 |
| Mean for 8 | 2.568 |


| Cation-cation |  |
| :--- | ---: |
| Si-SiA2 | $3.109(1)$ |
| M1-M1 | $3.290(1)$ |
| M1-SiA1 | 3.381 (1) |
| M1-SiA2 | $3.307(9)$ |

Table 3. Selected interatomic angles for $\mathrm{NaInSi}_{2} \mathrm{O}_{6}\left({ }^{\circ}\right)$

| Si tetrahedron |  | M1 octahedron |  | Chain angles |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| O1A1-Si-O2A1 | $115 \cdot 2$ (1) | O1A1-M1-O1B1 | $80 \cdot 5$ (1) | SiA1-O3A1-SiA2 | $140 \cdot 5$ (1) |
| O1A1-Si-O3A1 | 108.0 (2) | O1A1-M1-O2C1 | $91 \cdot 1$ (1) $\times 2$ | O3A2-O3A1-O3A2 | $170 \cdot 8$ (2) |
| O1A1-Si-O3A2 | 108.2 (2) | O1A1-M1-O1A2 | 88.9 (1) $\times 2$ | SiA1-O1A1-M1 | 122.5 (1) |
| O2A1-Si-O3A1 | $110 \cdot 4$ (1) | O1A1-M1-O1B2 | $81 \cdot 5$ (1) $\times 2$ | SiA2-O1A2-M1 | $121 \cdot 8$ (2) |
| O2A1-Si-O3A2 | $106 \cdot 0$ (1) | O1A2-M1-O2C1 | 92.8 (2) $\times 2$ | SiC1-O2C1-M1 | 144.1 (1) |
| O3A1-Si-O3A2 | 108.9 (1) | O1A2-M1-O2D1 | 95.5 (1) $\times 2$ | SiA1-O1A1-M2 | 114.7 (1) |
| Mean | 109.5 | O2C1-M1-O2D1 | 97.8 (1) | SiC2-O2C2-M2 | 98.3 (2) |
|  |  | Mean | 89.8 |  |  |

flexions and $3 \cdot 0 \%, 3 \cdot 1 \%$ for all measured reflexions respectively. A correction for isotropic extinction was made during the final stages of the refinement by including the coefficient (Zachariasen, 1968) as a variable. Final parameters are given in Table 1. Selected interatomic distances and angles are presented in Tables 2 and 3 respectively.*

Discussion. The variation in cell dimensions with M1 cation radius for the Na pyroxenes is shown in Fig. 1. It is apparent that the relatively small $a \sin \beta$ and $c$ dimensions in the In pyroxene contribute significantly to the anomalously small cell volume noted by Prewitt \& Shannon (1969). The length of the octahedral chain increases as the radius of the M1 cation increases from A1 to Sc ; this is accompanied by an increase in the length of the tetrahedral chain through extension of the $\mathrm{O}(3)-\mathrm{O}(3)$ edge and concomitant increase in the mean $\mathrm{Si}-\mathrm{O}(3)$ distance. In the In pyroxene, the mean $\mathrm{Si}-\mathrm{O}(3)$ distance is equal to that of the Sc pyroxene. Apparently the bonding requirements of the $O(3)$ anion allow no further extension of the tetrahedral chain, resulting in the smaller than expected $c$ dimension of the In pyroxene.

[^1]The M2-O(2) bond length is constant from A 1 to Sc , but decreases in the In pyroxene. This exerts a clamping effect on further increase in the $\mathbf{a}^{*}$ direction leading to an anomalously low value for $a \sin \beta$ (Fig. 1). This can be compared to the situation in the Li pyroxenes where M2-O(2) decreases across the series from A1 to Sc.

Interchain linkage is maintained during $b$ axis expansion by a combination of rotation of the tetrahedra about an axis parallel to $\mathbf{c}$ and distortion of tetrahedral edge lengths, both of which produce an enlargement in the mirror component of the $c$-gliderelated $\mathrm{O}(1)-\mathrm{O}(1)$ separation. No obvious constraints occur on either of these processes, and the $b$ axis increases normally throughout the whole series.
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[^0]:    Abstract. $\mathrm{NaInSi} \mathrm{O}_{6}, \mathrm{C} 2 / c$. Cell constants at $20^{\circ} \mathrm{C}$ with Мо $K \alpha(\lambda=0.71069 \AA): a=9.9023$ (4), $b=9.1307$ (4),

[^1]:    * A list of structure factors is available from the authors and has also been deposited with the British Library Lending Division as Supplementary Publication No. SUP 30389 (7 pp.). Copies may be obtained through: The Executive Secretary, International Union of Crystallography, 13 White Friars, Chester CH1 1NZ, England.

